



SLAB: A Certifying Model Checker for Infinite-State Concurrent Systems

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SLAB



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- which can produce **certificates** if the system is correct



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System Description:



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System Description:

- transition systems described by linear constraints



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- **infinite state** (real time, infinite datatypes, ...)
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- which can produce **certificates** if the system is correct

System Description:

- transition systems described by linear constraints
- safety properties



Certification



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Standard practice for model checkers

- Error found \implies Counterexample
- Error unreachable \implies "Correct"



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But model checker is just another piece of software...

- ... it may contain bugs!



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We need a **certificate as a proof** of correctness

- Should be independently and automatically checkable
- Provides higher degree of confidence in the verification results
- Helps understanding the reason of system correctness



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Certificates

- In graphical format
- In SMT-LIB format
- Independently checkable by standard SMT solvers



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Coming soon...

- Integration into theorem proving process
- Interfacing with Coq



SLAB Certificate Example



SLAB Certificate Example

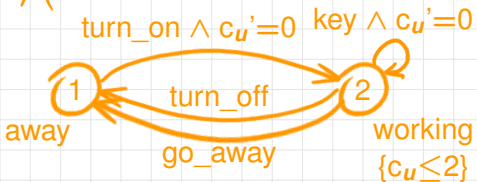




SLAB Certificate Example

c_u, c_L : clock

turn_on, key, ... : event

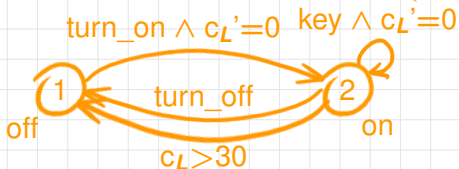
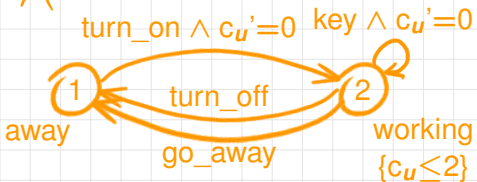




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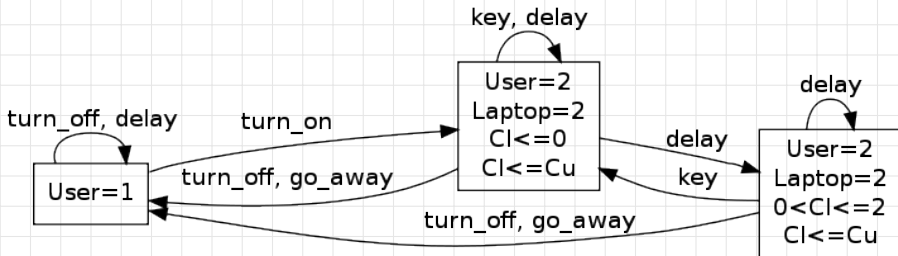
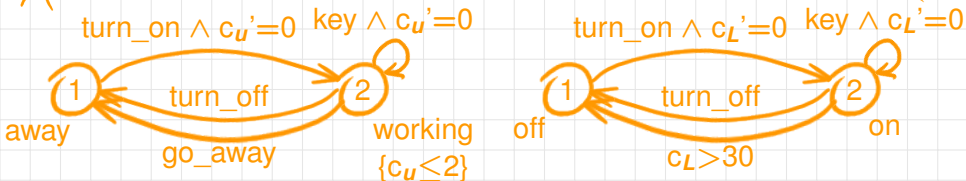




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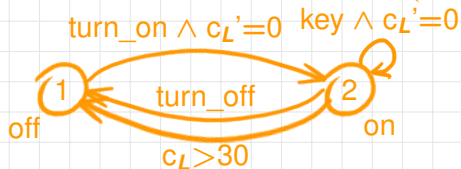
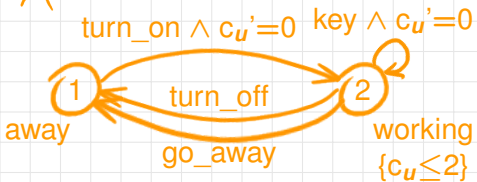
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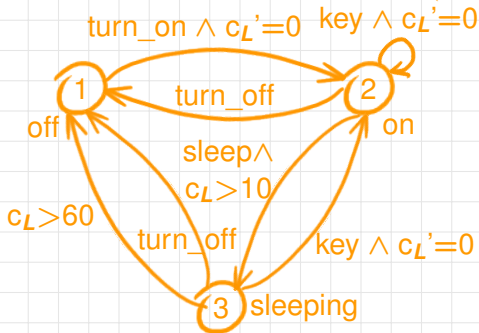
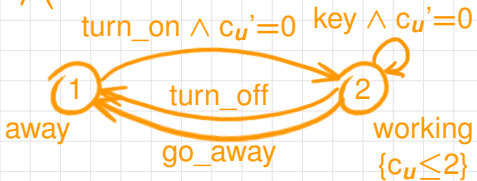


SLAB Certificate Example (2)



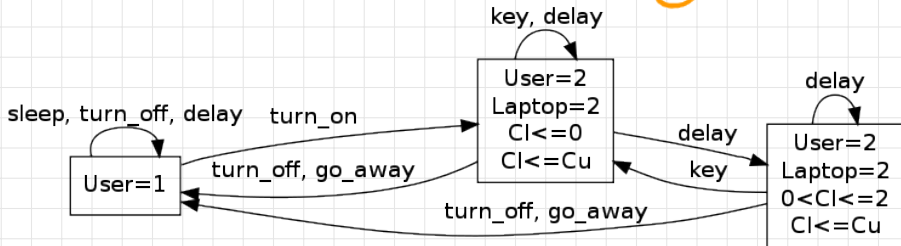
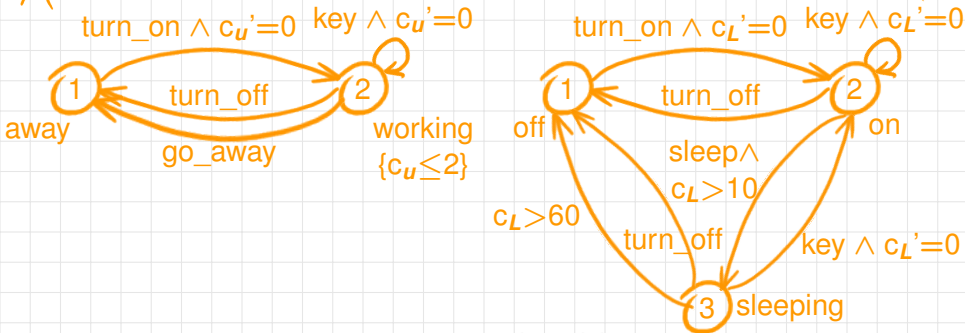


SLAB Certificate Example (2)





SLAB Certificate Example (2)





System and Certificate

Transition System $\mathcal{S} = (init, \mathcal{T}, error)$

- Initial condition $init(V)$
- Set of system transitions $\mathcal{T}: \tau_i(V, V')$
- Error condition $error(V)$
- $init, error, \tau_i$ are linear arithmetic constraints

Certificate $\mathcal{C} = (N, E, \varphi, \eta)$

- Finite graph with nodes N and edges E
- Node labeling: $\varphi : N \rightarrow Asrt(V)$
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System and Certificate

 $x, y : \mathbb{Z}$ $init : x = 0$

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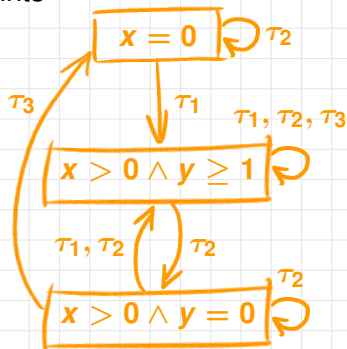
$\tau_2 : y' = x - 1$

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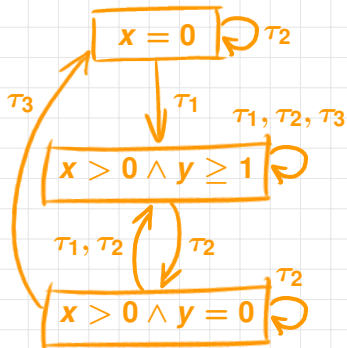
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Certificate Correctness

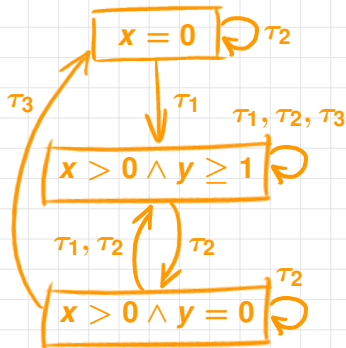
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- $\Phi = \bigvee_{n \in \mathbb{N}} \varphi_n$



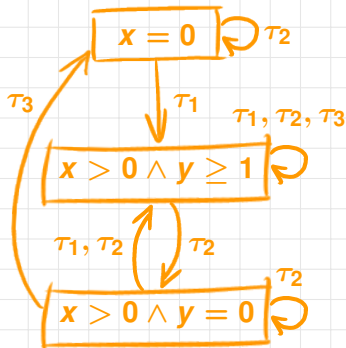


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Verification Conditions





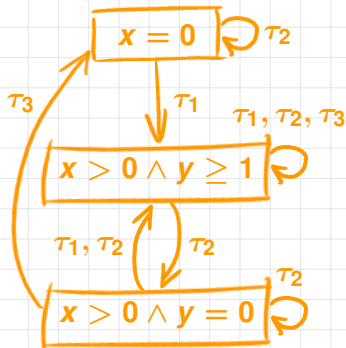
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- Initiation:
 $init \Rightarrow \Phi$





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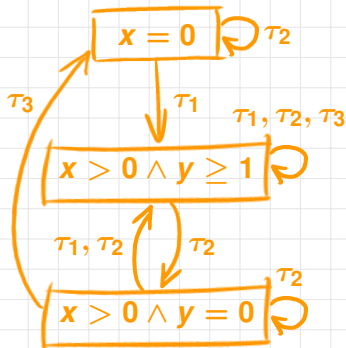
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Verification Conditions

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- Consecution:

 $\forall n \in N, \tau \in \mathcal{T} : \{\varphi_n\} \tau \{ \bigvee_{m \rightarrow n} \varphi_m \}$




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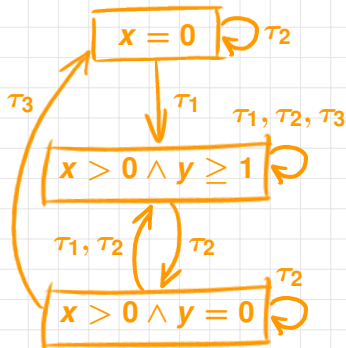
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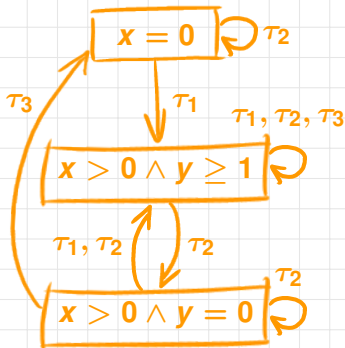
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- Error exclusion:

$$\Phi \Rightarrow \neg error$$





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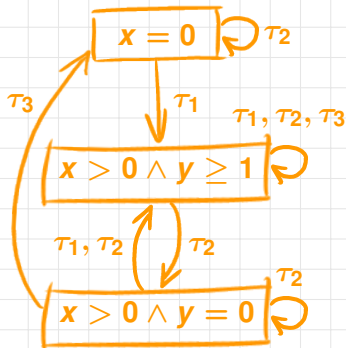
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Inductive Invariant

- $\Phi = \bigvee_{n \in \mathbb{N}} \varphi_n$

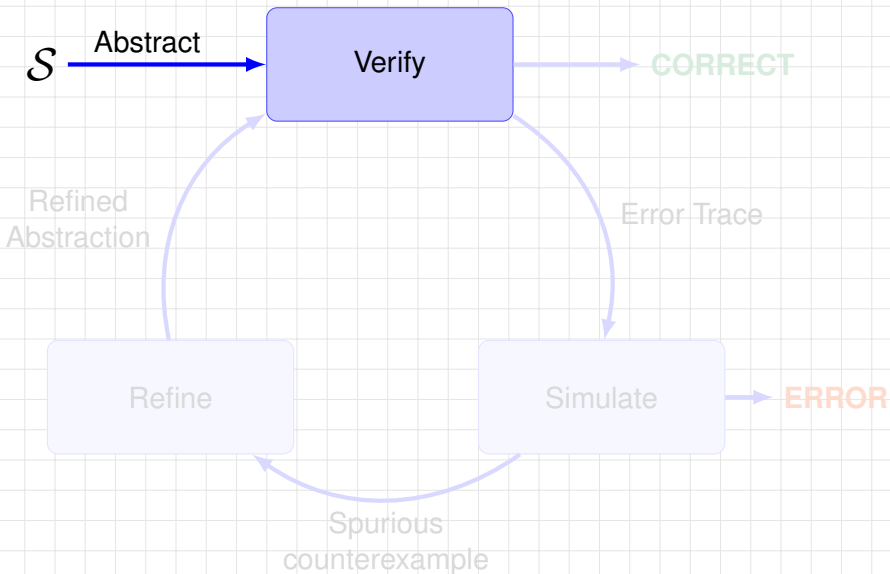
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- Initiation:
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 $\forall n \in \mathbb{N}, \tau \in \mathcal{T} : \{\varphi_n\} \tau \{\bigvee_{m \in \mathbb{N}} \varphi_m\}$
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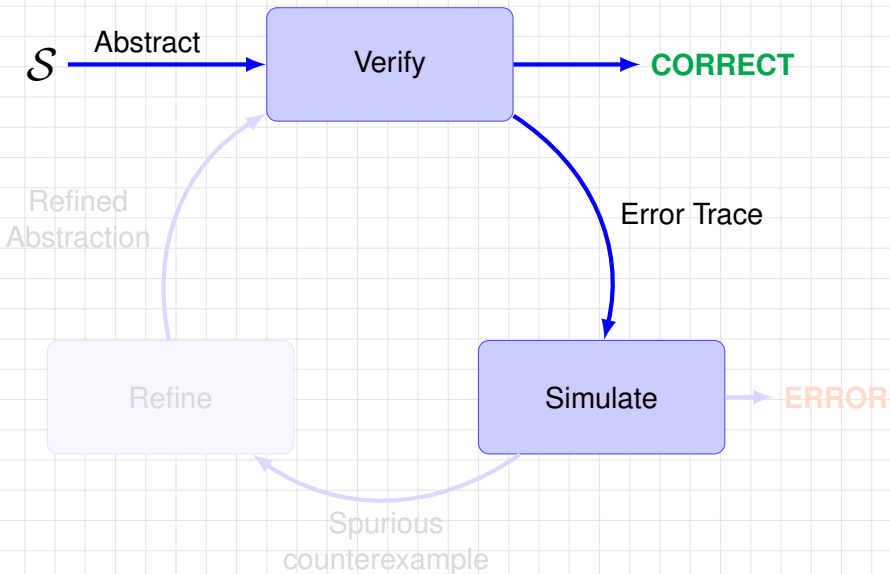


Counterexample-Guided Abstraction Refinement



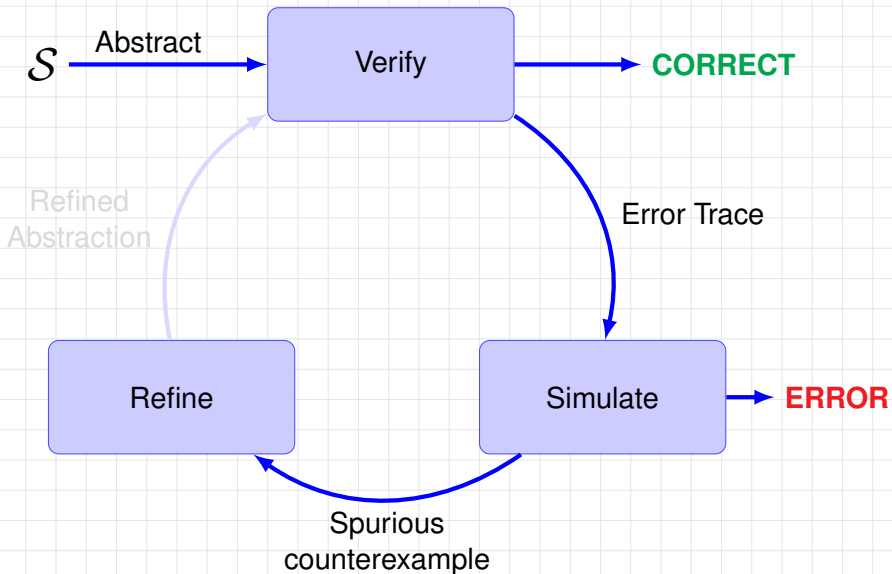


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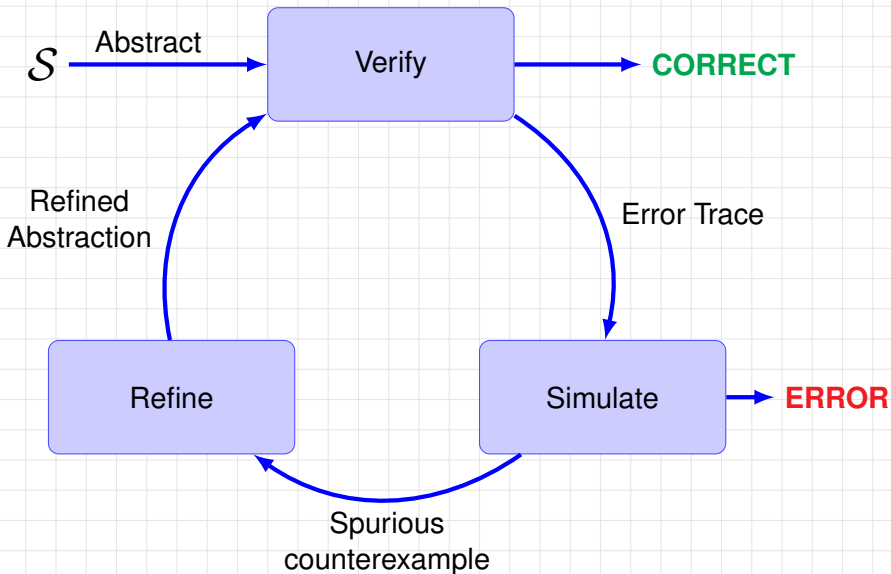


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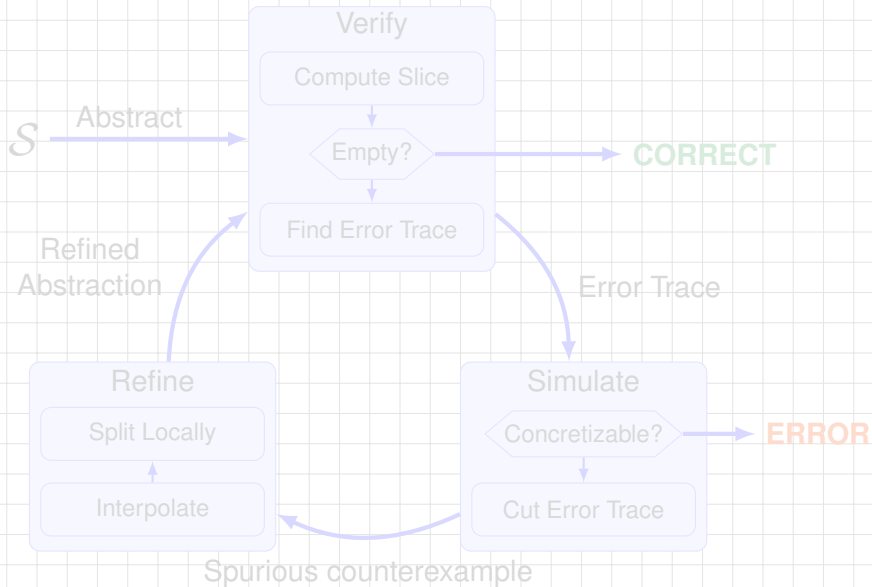


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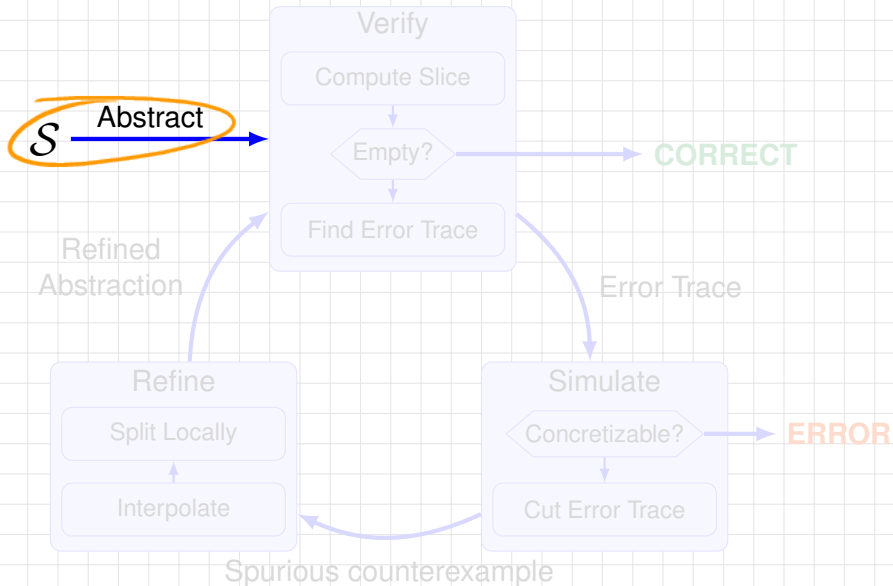


Slicing Abstraction Refinement





Slicing Abstraction Refinement





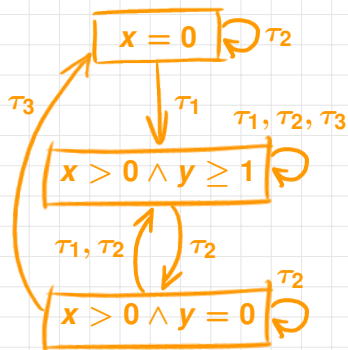
System and Certificate

Transition System $\mathcal{S} = (\text{init}, \mathcal{T}, \text{error})$

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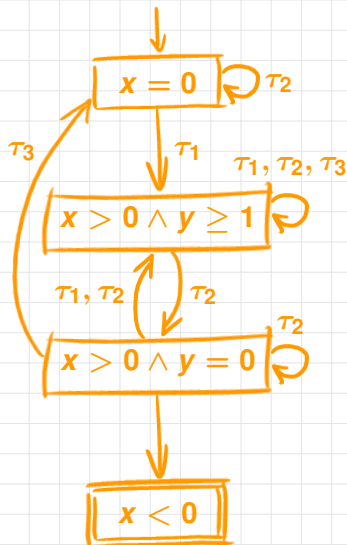
System and Abstraction

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- Set of system transitions $\mathcal{T}: \tau_i(V, V')$
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Abstraction $\mathcal{A} = (N, E, \varphi, \eta, I, F)$

- Finite graph with nodes N and edges E
- Node labeling: $\varphi: N \rightarrow \text{Asrt}(V)$
- Edge labeling: $\eta: E \rightarrow 2^{\mathcal{T}}$
- Initial nodes $I \subseteq N$, final nodes $F \subseteq N$





Initial Abstraction

- Initial abstraction over *init*, *error*

$\neg \text{init} \wedge \neg \text{error}$

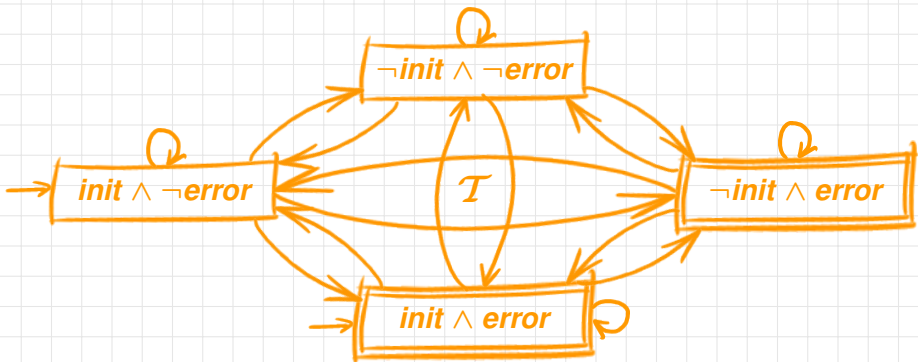
$\rightarrow \text{init} \wedge \neg \text{error}$

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Initial Abstraction

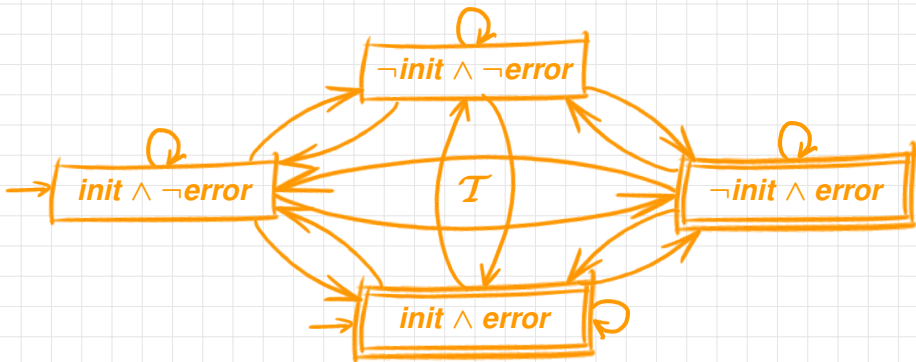
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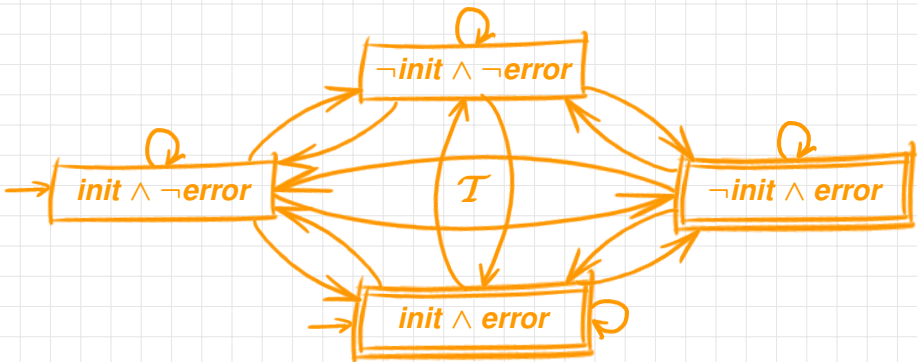
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- We need only *irreducible* error paths





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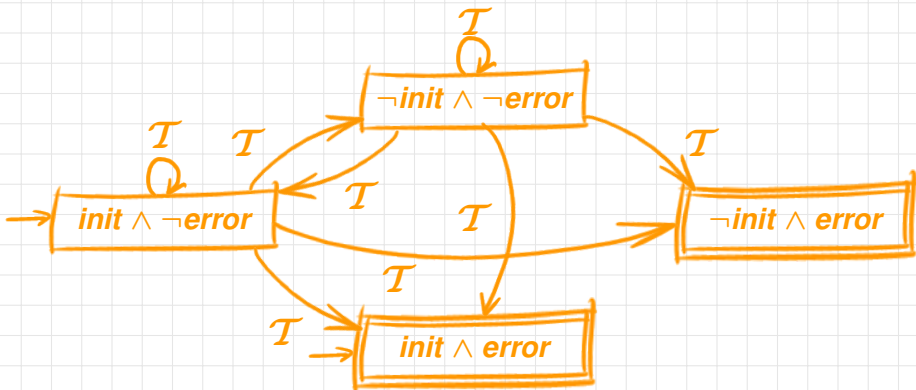
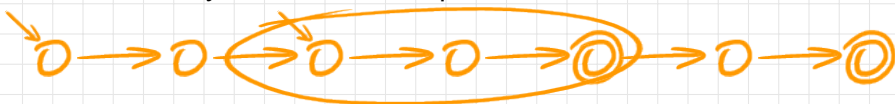
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Example: Initial Abstraction

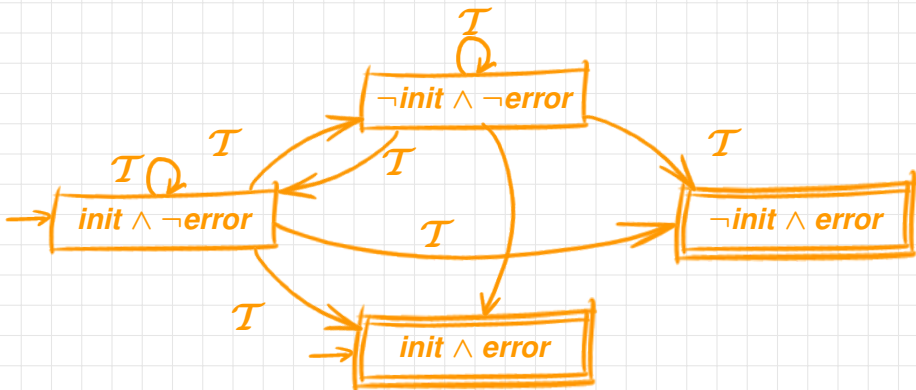
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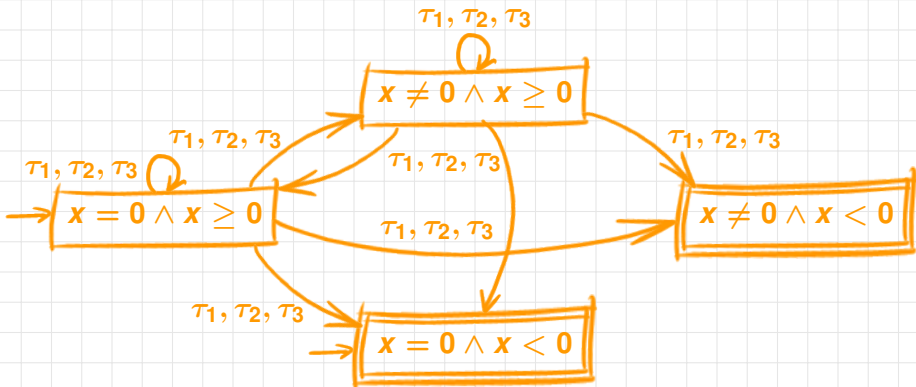
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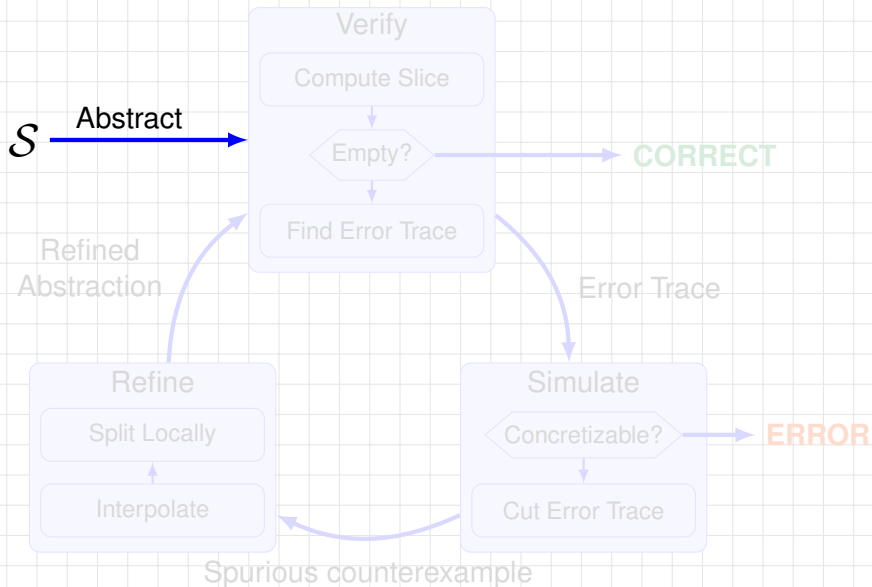
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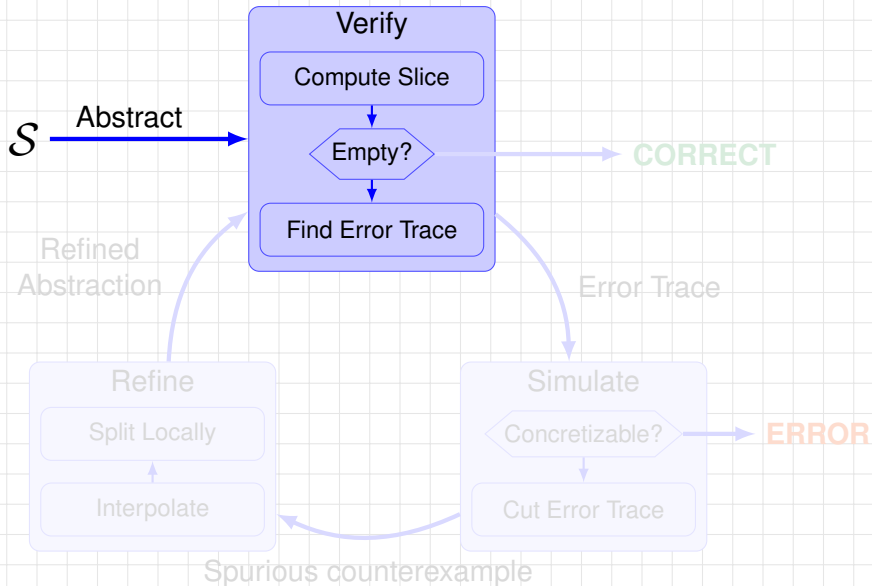


Slicing Abstraction Refinement



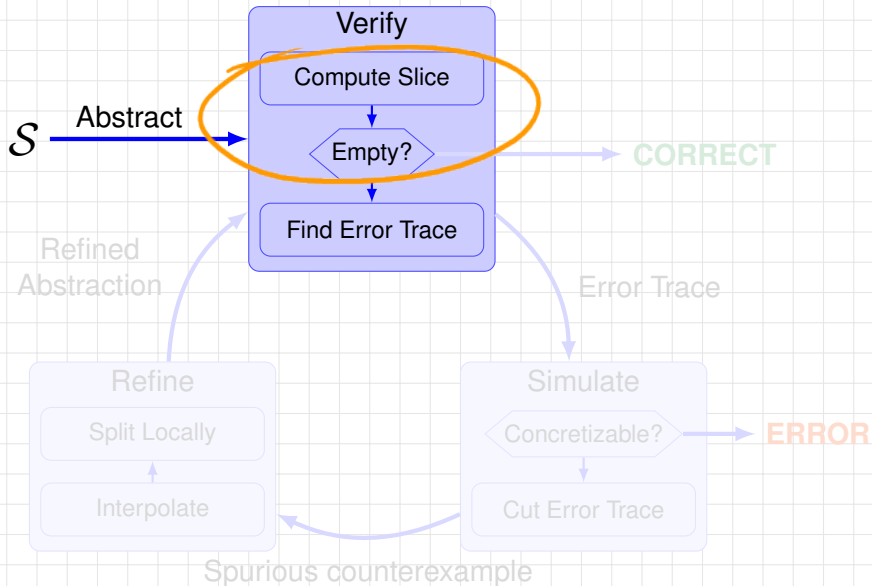


Slicing Abstraction Refinement





Slicing Abstraction Refinement





Slicing



Slicing

- Inconsistent nodes





Slicing

- Inconsistent nodes





Slicing

- Inconsistent nodes



- Unreachable nodes





Slicing

- Inconsistent nodes



- Unreachable nodes





Slicing

- Inconsistent nodes



- Unreachable nodes



- Inconsistent transitions





Slicing

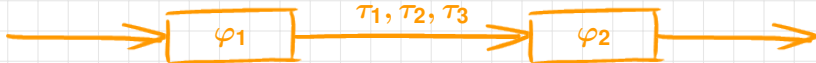
- Inconsistent nodes



- Unreachable nodes



- Inconsistent transitions



$\varphi_1 \wedge T_2 \wedge \varphi_2$ unsatisfiable



Slicing

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Slicing

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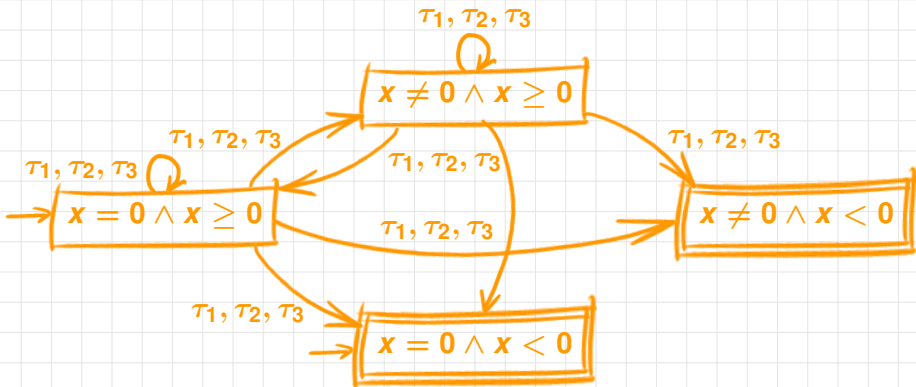
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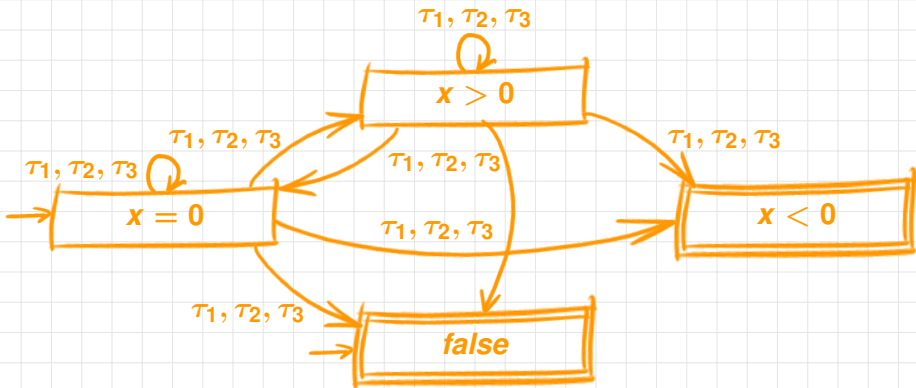
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Example: Slicing

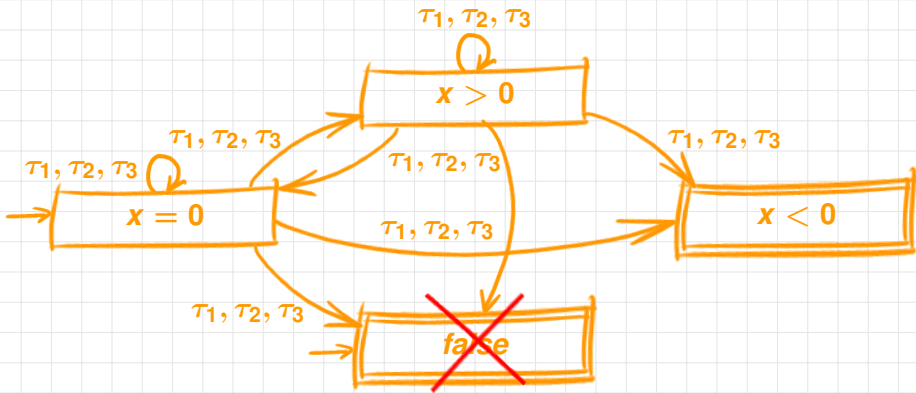
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$





Example: Slicing

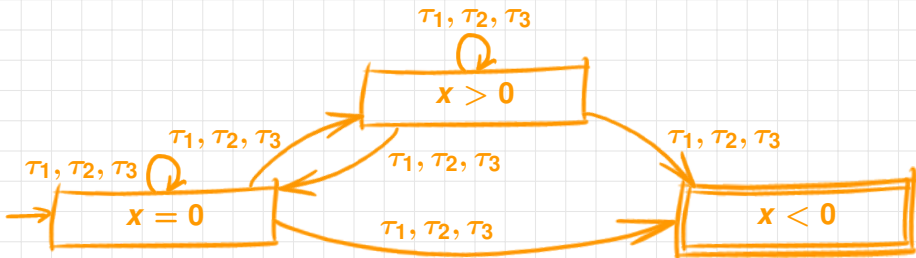
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$





Example: Slicing

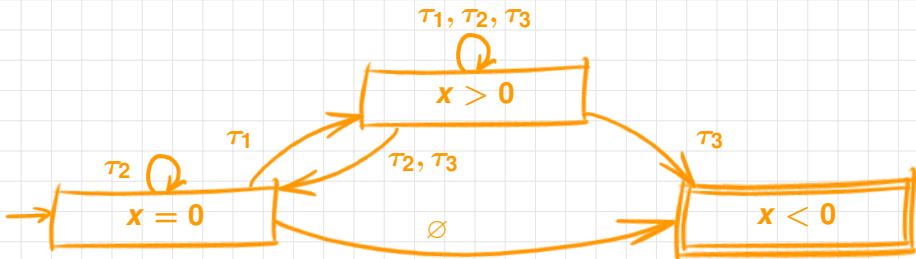
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$





Example: Slicing

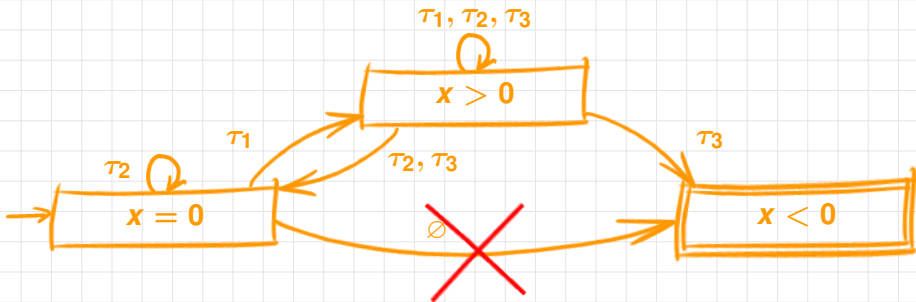
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$





Example: Slicing

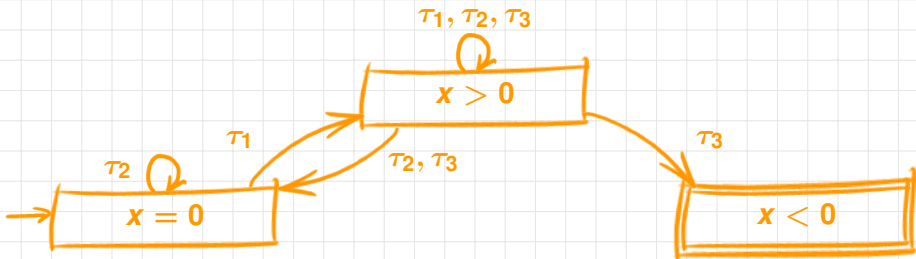
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

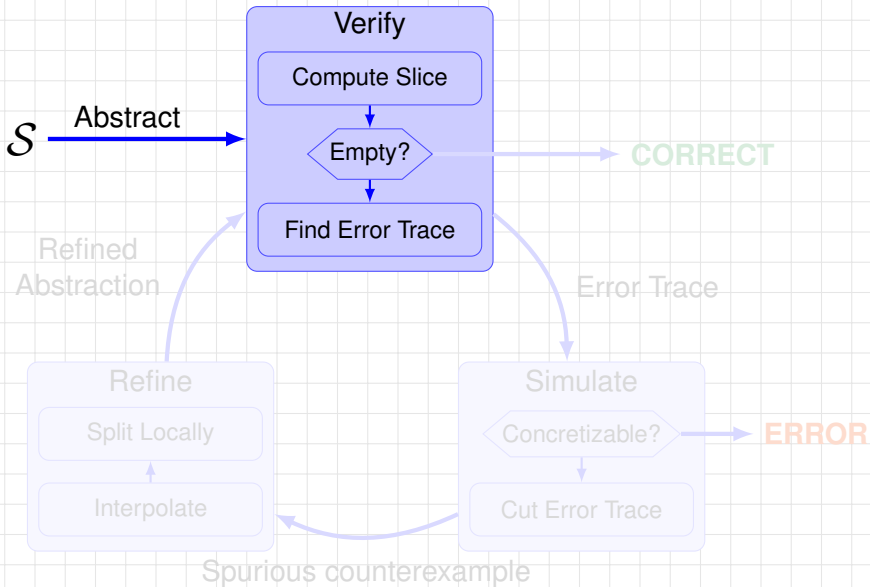
error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$



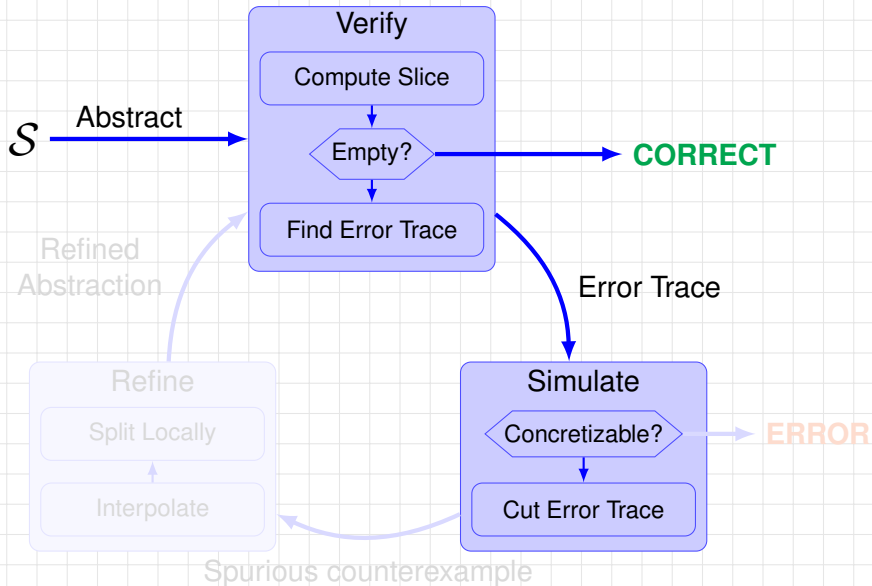


Slicing Abstraction Refinement



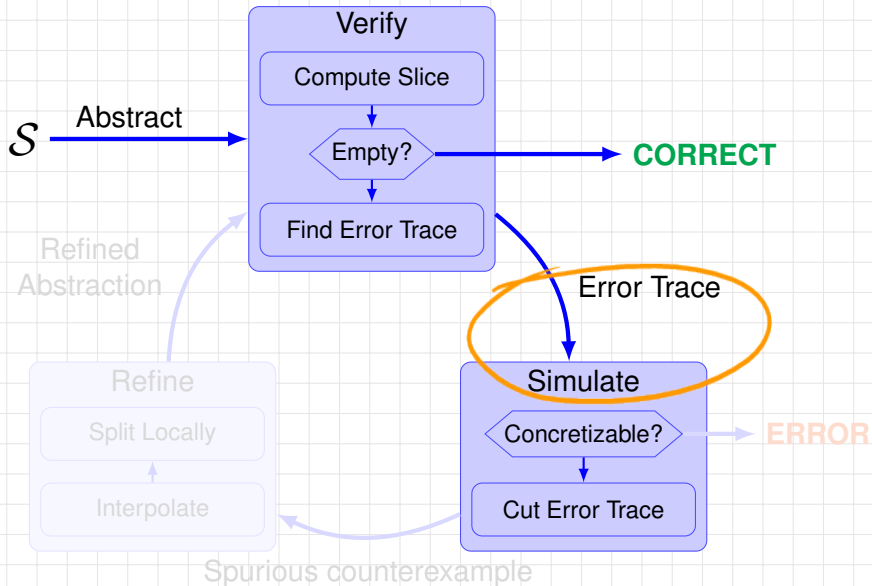


Slicing Abstraction Refinement





Slicing Abstraction Refinement





Example: Error Path Analysis

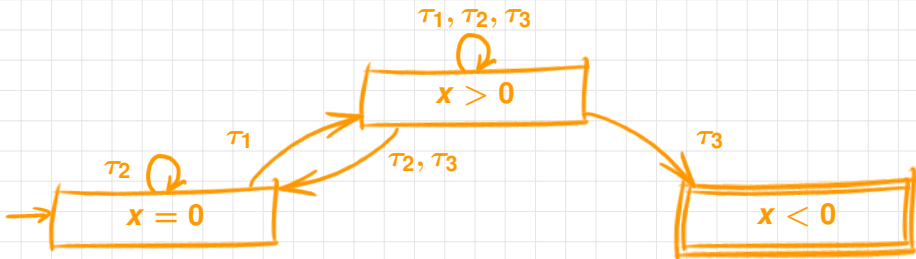
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

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Example: Error Path Analysis

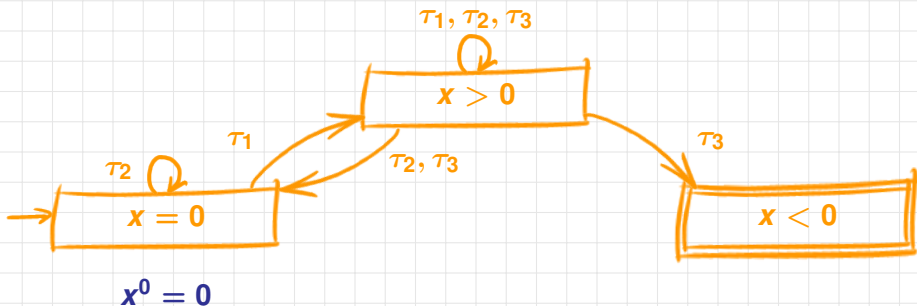
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

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τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$



$\Phi =$



Example: Error Path Analysis

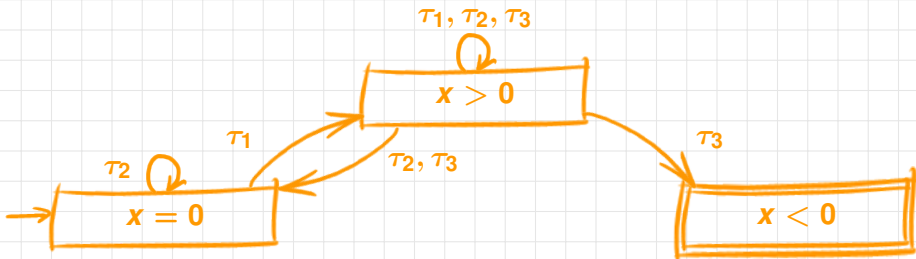
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$



$$x^0 = 0$$

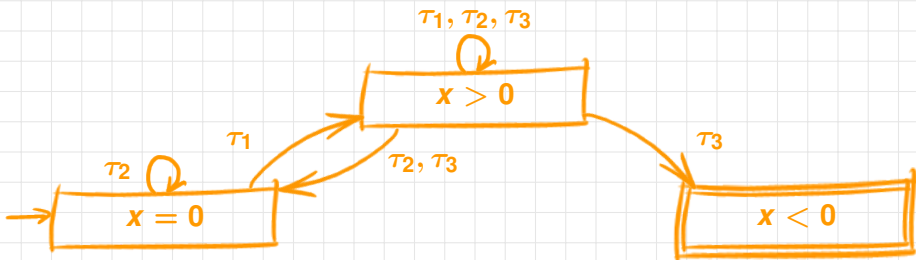
$\Phi =$

$$x^1 = 1 \wedge y^1 = x^0 + 1$$



Example: Error Path Analysis

$init : x = 0$
 $\tau_1 : x' = 1 \wedge y' = x + 1$
 $\tau_2 : y' = x - 1 \wedge x' = x$
 $error : x < 0$
 $\tau_3 : x \geq 1 \wedge x' = y \wedge y' = y$

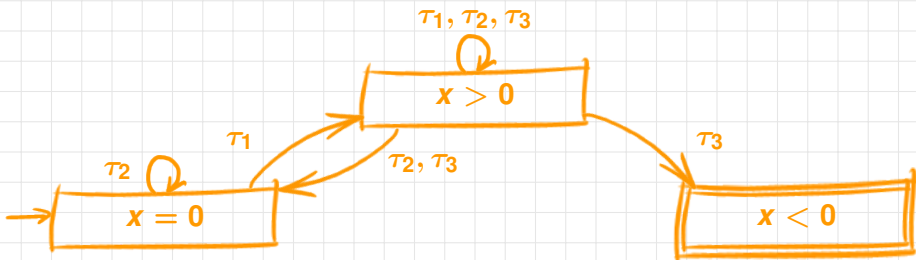


$$\Phi = \begin{array}{l}
 x^0 = 0 \qquad \qquad \qquad x^1 > 0 \\
 \wedge \\
 x^1 = 1 \wedge y^1 = x^0 + 1
 \end{array}$$



Example: Error Path Analysis

$init : x = 0$
 $\tau_1 : x' = 1 \wedge y' = x + 1$
 $\tau_2 : y' = x - 1 \wedge x' = x$
 $error : x < 0$
 $\tau_3 : x \geq 1 \wedge x' = y \wedge y' = y$

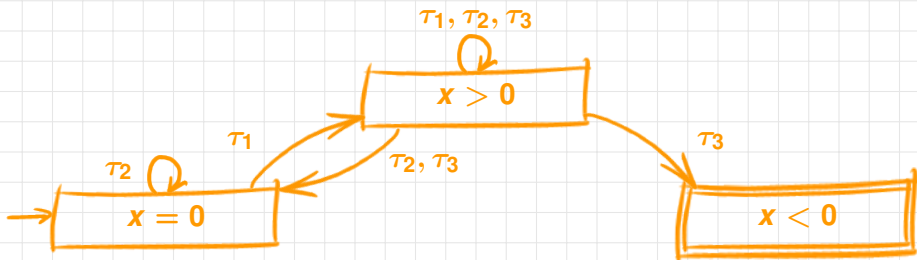


$$\begin{aligned}
 \Phi = & \quad x^0 = 0 & \quad x^1 > 0 \\
 & \quad \wedge & \quad \wedge \\
 & \quad x^1 = 1 \wedge y^1 = x^0 + 1 & \quad x^1 \geq 1 \wedge x^2 = y^1 \wedge y^2 = y^1
 \end{aligned}$$



Example: Error Path Analysis

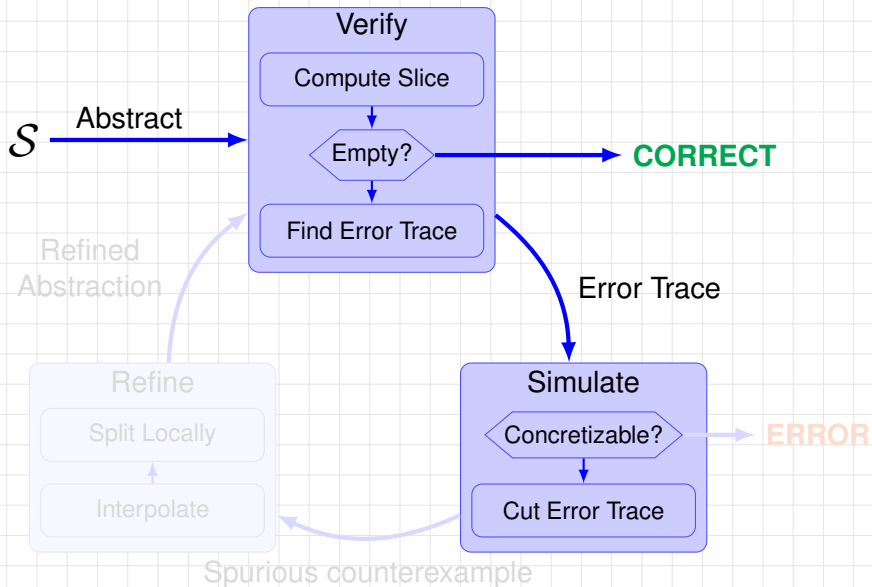
$init : x = 0$
 $\tau_1 : x' = 1 \wedge y' = x + 1$
 $\tau_2 : y' = x - 1 \wedge x' = x$
 $error : x < 0$
 $\tau_3 : x \geq 1 \wedge x' = y \wedge y' = y$



$\Phi =$
 $x^0 = 0$
 $x^1 > 0$
 $x^2 < 0$
 $x^1 = 1 \wedge y^1 = x^0 + 1$
 $x^1 \geq 1 \wedge x^2 = y^1 \wedge y^2 = y^1$

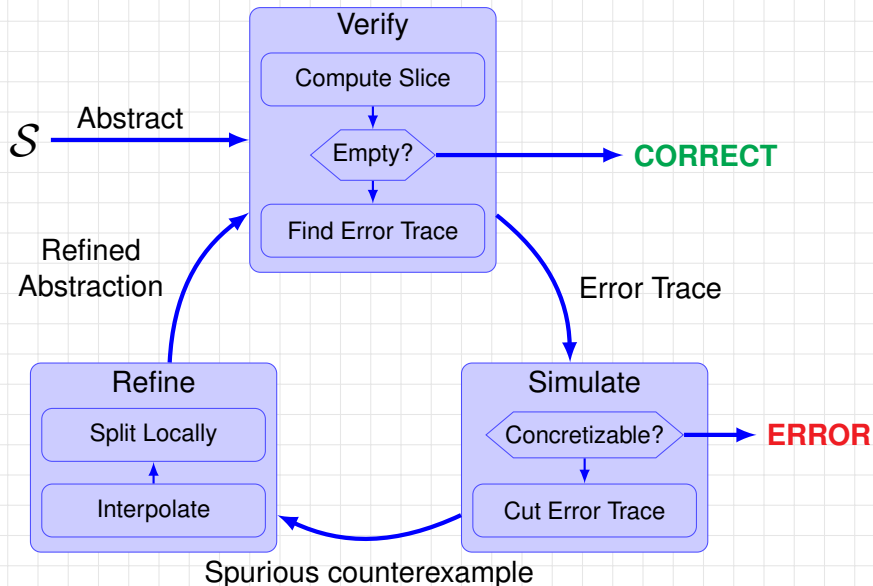


Slicing Abstraction Refinement



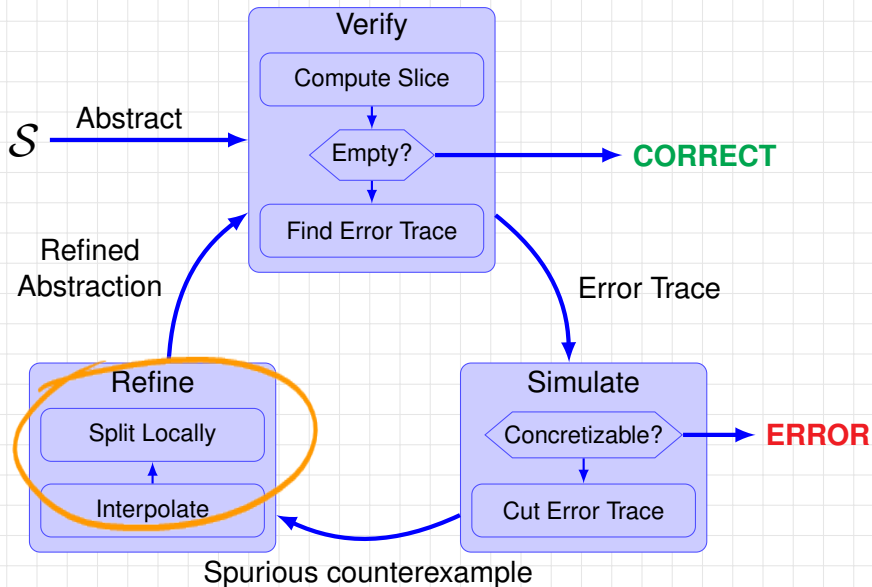


Slicing Abstraction Refinement





Slicing Abstraction Refinement





Abstraction Refinement



Abstraction Refinement

Spurious counterexample





Abstraction Refinement

Spurious counterexample

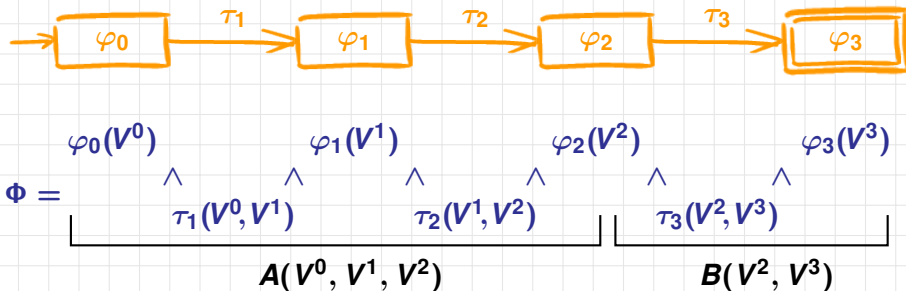


$$\Phi = \varphi_0(V^0) \wedge \tau_1(V^0, V^1) \wedge \varphi_1(V^1) \wedge \tau_2(V^1, V^2) \wedge \varphi_2(V^2) \wedge \tau_3(V^2, V^3) \wedge \varphi_3(V^3)$$



Abstraction Refinement

Spurious counterexample





Abstraction Refinement

Spurious counterexample



$$\Phi = \underbrace{\varphi_0(V^0) \wedge \tau_1(V^0, V^1) \wedge \varphi_1(V^1) \wedge \tau_2(V^1, V^2) \wedge \varphi_2(V^2)}_{A(V^0, V^1, V^2)} \wedge \underbrace{\tau_3(V^2, V^3) \wedge \varphi_3(V^3)}_{B(V^2, V^3)}$$

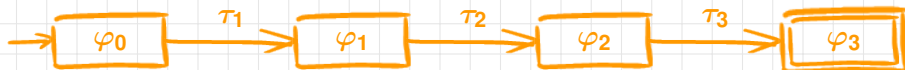
$A \wedge B$ unsat, but A, B sat \rightsquigarrow Craig interpolant η :

- $A \models \eta$
- $B \models \neg \eta$
- $\text{Var}(\eta) \subseteq \text{Var}(A) \cap \text{Var}(B)$



Abstraction Refinement

Spurious counterexample



$$\Phi = \underbrace{\varphi_0(V^0) \wedge \tau_1(V^0, V^1) \wedge \varphi_1(V^1) \wedge \tau_2(V^1, V^2) \wedge \varphi_2(V^2)}_{A(V^0, V^1, V^2)} \wedge \underbrace{\tau_3(V^2, V^3) \wedge \varphi_3(V^3)}_{B(V^2, V^3)}$$

$A \wedge B$ unsat, but A, B sat \rightsquigarrow Craig interpolant η :

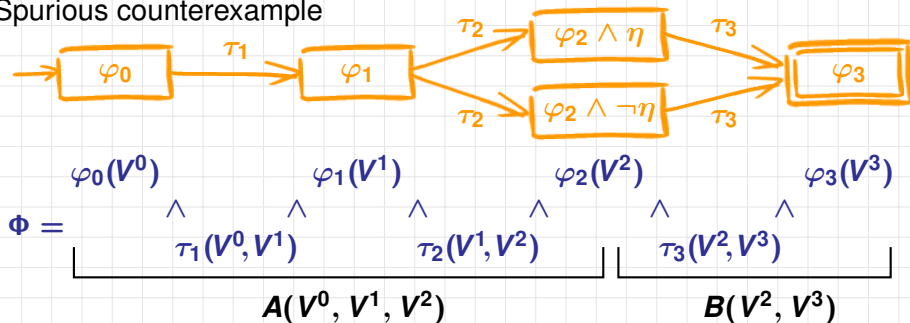
- $A \models \eta$
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- $\text{Var}(\eta) \subseteq \text{Var}(A) \cap \text{Var}(B)$

\rightsquigarrow split locally with $\eta, \neg \eta$



Abstraction Refinement

Spurious counterexample



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\rightsquigarrow split locally with $\eta, \neg \eta$



Example: Abstraction Refinement

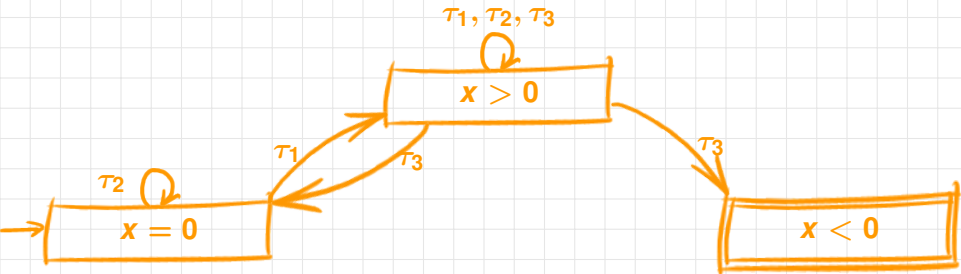
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$



$x^0 = 0$

$x^1 > 0$

$x^2 < 0$

$\Phi =$

\wedge

\wedge

\wedge

\wedge

$x^1 = 1 \wedge y^1 = x^0 + 1$

$x^1 \geq 1 \wedge x^2 = y^1 \wedge y^2 = y^1$



Example: Abstraction Refinement

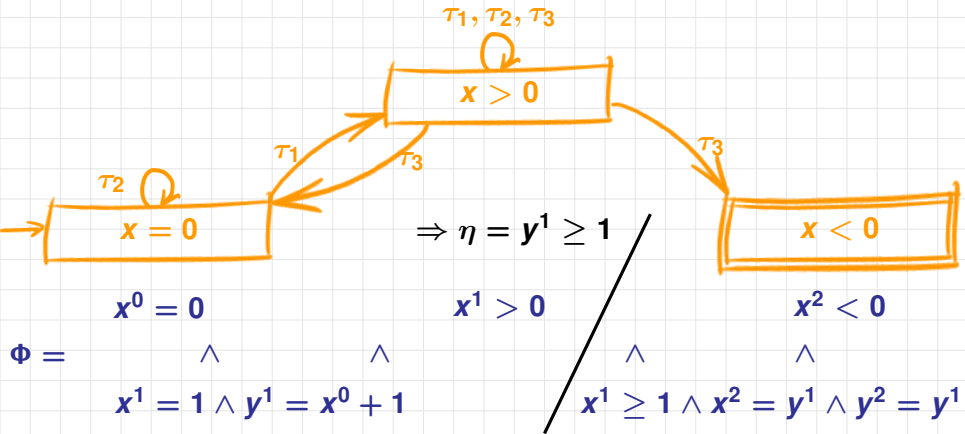
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

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Example: Abstraction Refinement

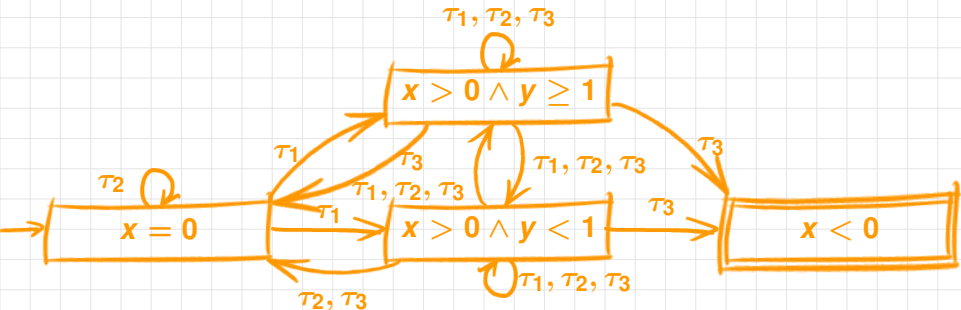
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$





Example: Slicing (2)

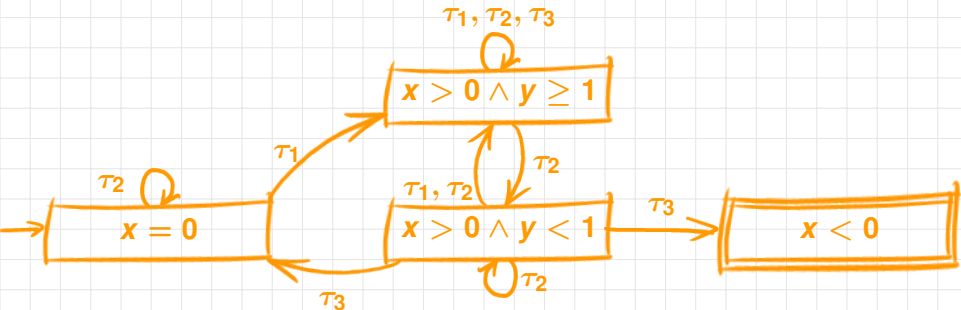
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

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τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$



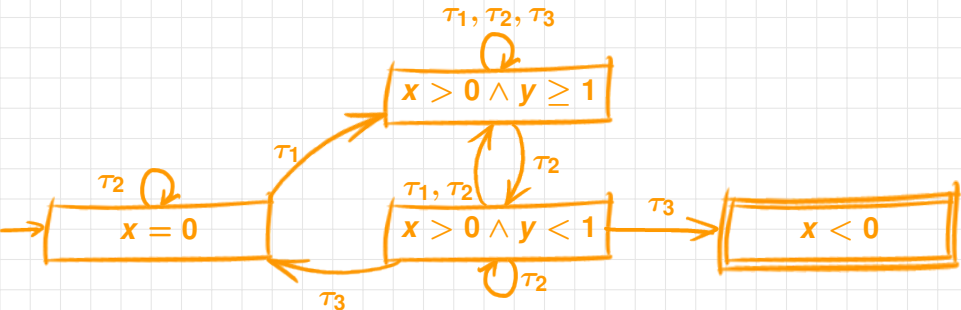


Example: Abstraction Refinement (2)

$\tau_1 : x' = 1 \wedge y' = x + 1$
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 $\tau_3 : x \geq 1 \wedge x' = y \wedge y' = y$

init : $x = 0$

error : $x < 0$





Example: Abstraction Refinement (2)

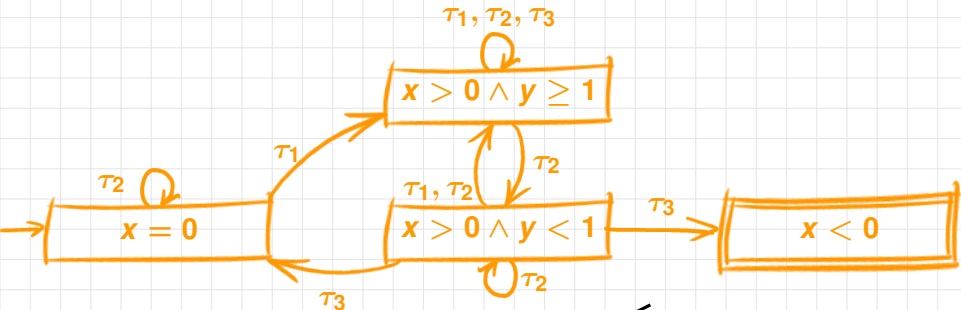
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

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error : $x < 0$

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$\Rightarrow \eta = y^2 \geq 0$

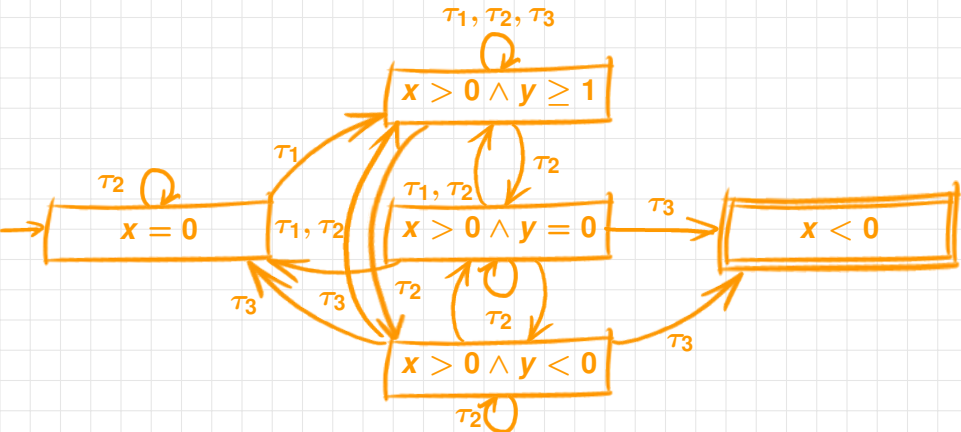


Example: Abstraction Refinement (2)

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init : $x = 0$

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Example: Slicing (3)

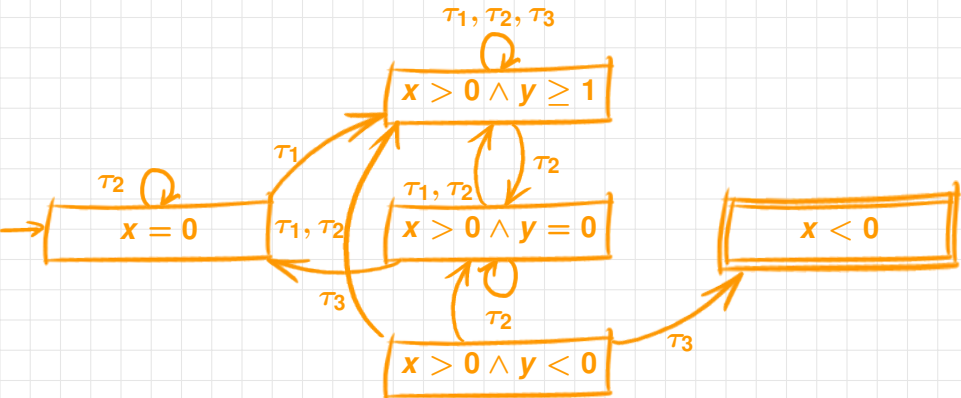
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

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τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$





Example: Slicing (3)

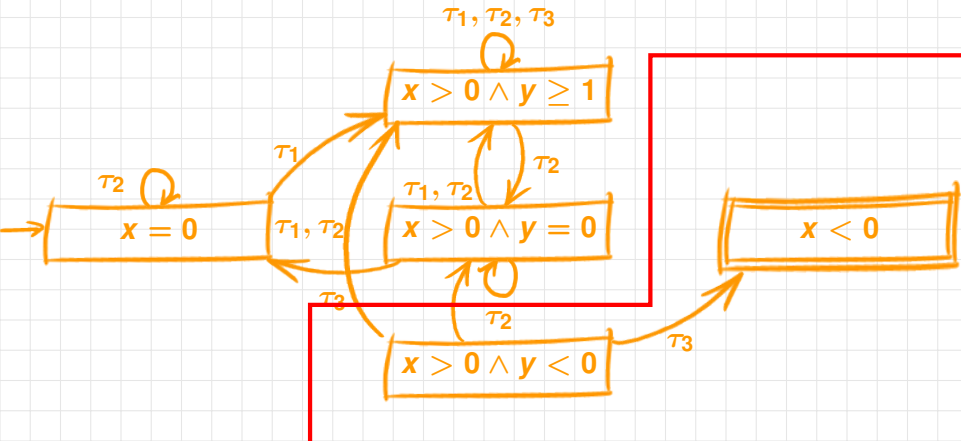
init : $x = 0$

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τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$





Example: Certificate

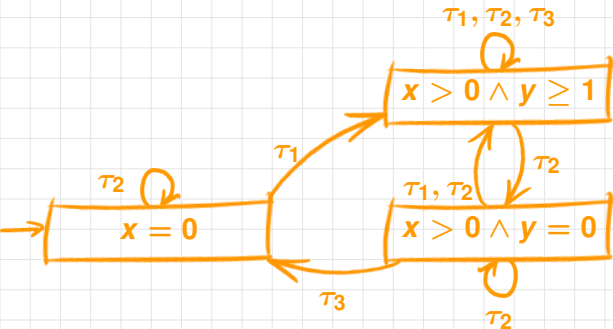
init : $x = 0$

τ_1 : $x' = 1 \wedge y' = x + 1$

τ_2 : $y' = x - 1 \wedge x' = x$

error : $x < 0$

τ_3 : $x \geq 1 \wedge x' = y \wedge y' = y$





Demo



Summary



Summary

SLAB is a Model Checker for:

- **infinite state** (real time, infinite datatypes, ...)
- **concurrent systems** (communication protocols, control systems,...)
- which can produce **certificates** if the system is correct



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Certificates

- In graphical format
- In SMT-LIB format
- Independently checkable by standard SMT solvers
- Coming soon: interface with Coq theorem prover



Summary

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Thank you for attention!