

## Verification

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### Problem 1: Cooper's Method [8 Points]

Apply quantifier-elimination to the following  $\Sigma_{\mathbb{Z}}$ -formulae.

- a)  $\forall y. 3 < x + 2y \vee 2x + y < 3$
  - b)  $\exists y. 3 < x + 2y \vee 2x + y < 3$
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The following exercises belong to the afternoon session.

### Problem 2: Congruence Closure Algorithm [8 Points]

Apply the decision procedure for  $T_E$  to the following  $\Sigma_E$  formulae:

- a)  $f(f(f(a))) = f(a) \wedge f(f(a)) = a \wedge f(a) \neq a$
- b)  $f(f(f(a))) = f(f(a)) \wedge f(f(f(f(a)))) = a \wedge f(a) \neq a$
- c)  $f(g(x)) = g(f(x)) \wedge f(g(f(y))) = x \wedge f(y) = x \wedge g(f(x)) \neq x$
- d)  $p(x) \wedge f(f(x)) = x \wedge f(f(f(x))) = x \wedge \neg p(f(x))$