

Verification

Problem 1: Decision Procedures [8 Points]

1. Apply the DAG-based decision procedure for T_E to the following Σ_E -formulae.

a) $f(f(f(a))) = f(f(a)) \wedge f(f(f(f(a)))) = a \wedge f(a) \neq a$

b) $f(g(x)) = g(f(x)) \wedge f(g(f(y))) = x \wedge f(y) = x \wedge g(f(x)) \neq x$

2. Apply the decision procedure for T_{cons} to the following T_{cons} -formulae:

c) $\text{car}(x) = y \wedge \text{cdr}(x) = z \wedge x \neq \text{cons}(y, z)$

c) $\neg \text{atom}(x) \wedge \text{car}(x) = y \wedge \text{cdr}(x) = z \wedge x \neq \text{cons}(y, z)$